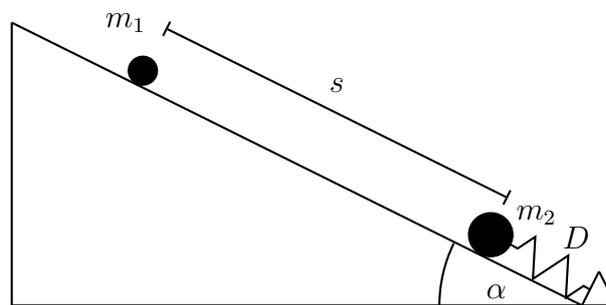


1. Exercise:



Consider two masses  $m_1 = 1.0 \text{ kg}$  and  $m_2 > m_1$  at distance  $s = 12 \text{ m}$  on a frictionless inclined plane with angle  $\alpha = 45^\circ$ . Both masses are initially at rest but are subject to gravity ( $g = 10 \frac{\text{m}}{\text{s}^2}$ ). The position of the second mass  $m_2$  is fixed by a spring with constant  $D$ . The goal is to find the maximum height  $h_1$  of the mass  $m_1$  and the maximum compression  $s_2$  of the spring after a total elastic collision.

(a) What would be the downward force acting on the mass  $m_1$ ?

$$F_D =$$

(b) From Newton's 2<sup>nd</sup> axiom state the acceleration of the mass  $m_1$

$$a =$$

(c) This means that the first mass performs a

- uniform motion       motion with constant acceleration       circular motion

(d) How depends the position of the first mass in general?

$$x(t) =$$

(e) Specify the integration variables.

$$v_0 =$$

$$x_0 =$$

(f) What would be the position of the mass  $m_1$  at the collision for this choice?

$$x(t) =$$

(g) Solve the equation for the position for this value to the time in order to determine the time  $t$  when both masses collide.

$$t =$$

(h) Find the velocity  $v$  before the collision by taking the time derivative of the position function and put the last value in.

$$v =$$

(i) State the laws of momentum and energy conservation for the elastic collision in the case that the second mass is initially at rest.

$$=$$

$$=$$

(j) Solve the law of momentum conservation to  $v'_2$ , the velocity of the second mass  $m_2$  after the collision.

$$v'_2 =$$

(k) Put this expression into the law of energy conservation and simplify it to a quadratic expression for  $v'_1$ , the velocity of the mass  $m_1$  after the collision.

$$0 =$$

- (l) Use the solution formula of quadratic expressions to obtain two solutions. Simplify them!

(1) :  $v'_{1,1} =$

(2) :  $v'_{1,2} =$

- (m) Which solution describes the situation before the collision?

- (n) Take the other expression and evaluate it for  $m_2 = 2$  kg and the given values.

$$v'_1 =$$

- (o) Put this value in the formula for  $v'_2$  in order to determine the velocity of the second mass after the collision.

$$v'_2 =$$

- (p) Now state the law of energy conversion which determines the maximum height  $h_1$  of the first mass if it has a velocity  $v'_1$ . Take as zero point of the potential energy the one at the position of the collision.

$$=$$

- (q) Solve this equation to  $h_1$ .

$$h_1 =$$

- (r) Put in the values calculated for  $v'_1$ .

$$\underline{\underline{h_1 =}}$$

- (s) Write down the law of energy conversion for the second mass when hitting the spring on the inclined plane if it has the velocity  $v'_2$ . Do not forget the potential energy caused by the difference in height  $h_2$ .

$$=$$

- (t) Express therein the difference in height by the compression of the spring.

$$=$$

(u) Rewrite this equation to a quadratic expression for the compression  $s_2$ .

$$0 =$$

(v) Solve the equation to the two mathematical solutions.

(I) :  $s_{2,1} =$

(II) :  $s_{2,2} =$

(w) Which solution is the physical solution?

(x) Put in this expression the spring constant  $D = 10^2 \frac{\text{N}}{\text{m}}$  and the values determined above.

$$\underline{\underline{s_2 =}}$$